

## Geometric average in time, discretely sampled

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$$Y_{ave} = (Y - \frac{1}{2}\sigma^2) \frac{t_1 + t_n}{2}$$

$$\sigma_{ave} = \sigma \sqrt{\frac{t_1(4n + 1) + t_n(2n - 1)}{t_n 6n}}$$

The geometric average in time of geometric Brownian motion is lognormal distributed.

These equations express the two parameters of the lognormal distribution as a function of the discretely sampled geometric average. The first averaging point is "t1", the last "tn", and the total number of averaging points is "n".

An application is the Vorst model for Asian options. In this model the arithmetic average of the Asian options is approximated with a geometric average.

### Symbol list:

Y	yield of the underlying
$Y_{ave}$	Effective yield of the average of the underlying
$\sigma$	Volatility of the underlying
$\sigma_{ave}$	Effective volatility of the average of the underlying
n	Number of averaging points
$t_1$	Time of the first average
$t_n$	Time of the last average