

Probability density of geometric Brownian motion at a fixed time

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$$P(S_t) = \frac{1}{S_t \sigma \sqrt{2\pi t}} \exp \frac{-(\ln S_t/S_0 - [\mu - \frac{1}{2}\sigma^2]t)^2}{2\sigma^2 t}$$

This equation gives the probability density function of an underlying S at some future time t. The underlying behavior is geometric Brownian motion, has a present value S₀, a yield (drift) of \mu, and volatility \sigma.

The probability density function is has a lognormal distribution with mean \mu.

Symbol list:

- $P(x)$ Probability of x
- S_t The value of the geometric Brownian motion process at time t
- σ Volatility of the geometric Brownian motion
- μ Drift of the geometric Brownian motion